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3 (Sem 1) PHY M2

2015

PHYSICS

(Major)

Paper : 1.2

Full Marks – 60

Time – Three hours

The figures in the margin indicate full marks for the questions.

SECTION – I

Marks – 40

1. (a) What do you mean by sharpness of resonance? 1
- (b) If a parameter whose unit is *meter* is Fourier Transformed what will be the unit in the Fourier plane? 1

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- (c) Plot the first two cycle of the wave starting from $t = 0$ represented by the wave equation

$$x = a \sin \left(\omega t + \frac{\pi}{4} \right). \quad 1$$

- (d) What is the mean free path of sound wave in a room if the dimension of the room is $6 \times 4 \times 5 \text{ m}^3$? Velocity of sound in the room is 350 m/s . 1

2. Answer any *two* questions : 6×2=12

- (a) What are the characteristics of wave motion? A simple harmonic wave is represented by

$$y = 100 \sin \left(\frac{2\pi t}{T} + \alpha \right) \text{ and the time period is}$$

30 sec . At time $t=0$, the displacement is 50 cm .

- (i) Calculate the phase angle at 7.5 sec .

- (ii) Phase difference between two positions at an interval of 6 sec . 2+4=6

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- (b) Write the properties of wave.

Two transverse sine wave of 4 mm wavelength $2\pi \text{ m}$ are in phase at $x = 0$, $t = 0$. Write the equation of the resultant wave. Find the maximum displacement and positions of the node.

- (c) Show that in forced vibration, the amplitude R is inversely proportional to the square of the driving force.

3. Answer any *three* questions

- (a) Show that the composition of two simple harmonic vibrations of the same period and amplitude with phase difference α forms an ellipse. If the period of the two waves is 2π and the phase angle between the two waves is $\frac{\pi}{2}$, find the equation of the ellipse with the x -axis when $t = 0$.

Explain how the frequency of the resultant wave can be determined using the above method.

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- (b) Show that for a series LCR circuit, the discharging is of simple harmonic type when

$$\frac{R^2}{4L^2} < \frac{1}{LC} \text{ with natural frequency}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{1}{LC} - \frac{R^2}{4L^2}}$$

A condenser of capacity $1\mu\text{F}$, and inductance of 0.2H and a resistance of 800Ω are connected in series. Check whether the circuit is oscillatory. $7+1=8$

- (c) Why the Laplace correction is required in the formulation of velocity of sound. Derive the formula for the velocity of sound in air by incorporating the Laplace correction.

Calculate the increase in velocity of sound in air per degree Celsius rise in temperature.

$$1+4+3=8$$

- (d) Consider a periodic function of the form with time period T and amplitude a

$$f(t) = a \left(1 - \frac{t}{T} \right) \text{ for } 0 < t < T$$

express the above function in Fourier series. Plot first three terms of the Fourier series.

$$5+3=8$$

- (e) The displacement $y(x, t)$ along transverse d

following wave eq

where $v = \sqrt{\frac{T}{\mu}}$ repre

transverse wave. T b string and μ , the mas the displacement $y(x, t)$ the following bounda

- (i) $y = 0$ at $x = 0$ and of t

- (ii) At $t = 0$

(a) $\frac{\partial y}{\partial t} = 0$ for a

(b) $y(x, t = 0) =$

$$y(x, t = 0) = \frac{a}{L}$$

where L is the l
d is the displace
distance a from

SECTION - II

Marks - 20

4. (a) What is achromatic doublet ? 1
- (b) What do you mean by circle of least confusion? 1
- (c) Under what condition the matrix method can be applied to an optical system ? 1
- (d) Name one aberration each suffered by image when the point object is on-axis and off-axis for a lens. 1

5. Answer any *one* question : $4 \times 1 = 4$

- (a) Find the matrix for a spherical surface of radius of curvature R separated by two media with refractive indices n_1 and n_2 when the object is placed in the first medium at a distance u from the surface. 4
- (b) Derive the lens formula for thin lens using Fermat's principle. 4

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6. Answer any *two* questions

- (a) Find the equivalent focal length of a lens with focal lengths f_1 and f_2 separated by a distance d . Hence find the position of the second principal point.
- (b) Show that the chromatic aberration of a lens (made of same material) is zero when the object is at a distance equal to the sum of the focal lengths of the two surfaces.
- (c) A thick equi-convex lens of refractive index n and thickness t is placed between two media of refractive indices n_1 and n_2 . Obtain the system focal length and principal points.

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